

A Computational Account of Opaque Phonological Interactions

Jane Chandlee

Haverford College

University of Chicago

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Outline

- ▶ Establish a framework for classifying phonological maps based on their computational complexity.
 - ▶ Subregular hierarchy of function classes: ISL, OSL, TSL
- ▶ Use this framework to present a computational analysis of *opaque phonological generalizations*.
 - ▶ 7 distinct cases of opacity are shown to be ISL functions.

Maps versus formal languages

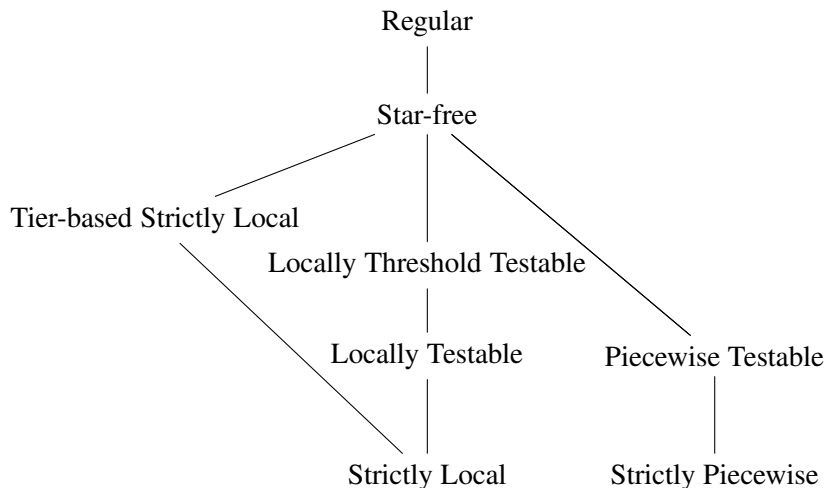
Formal Language	Map
{at, ap, am, ada, ...}	{(ad, at), (ab, ap), (am, am), (ada, ada)...}

- ▶ A formal language is a set of well-formed strings, according to some constraint(s) or grammar.
- ▶ Maps are functions that associate input strings to output strings.
- ▶ Analogous to the distinction between phonotactics and the UR to SR transformation.

Computational complexity of phonological patterns

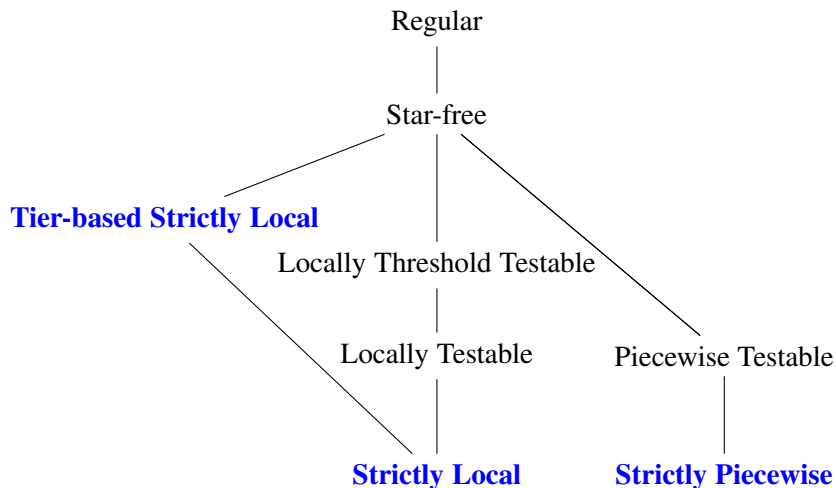
- ▶ What do we know about the computational complexity of phonotactics and phonological maps?
- ▶ Starting point: both are *regular* (i.e., finite state describable)
- ▶ Proposal: both are in fact *subregular* (i.e., describable with proper subsets of regular)
- ▶ Why is this restriction desirable?
 - ▶ Better fit to the typology
 - ▶ Learnability advantages

Subregular hierarchy of languages



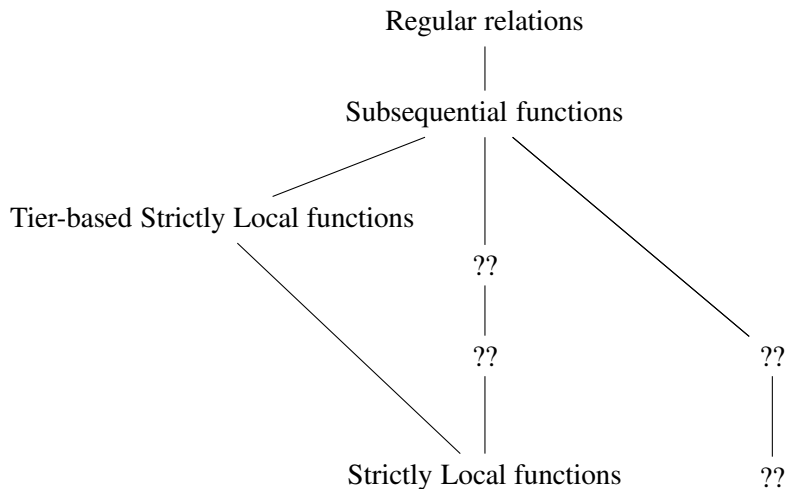
(Rogers and Pullum, 2011; Rogers et al., 2013; Heinz, 2010; Heinz et al., 2011; McMullin, 2016)

Subregular hierarchy of languages



(Rogers and Pullum, 2011; Rogers et al., 2013; Heinz, 2010; Heinz et al., 2011; McMullin, 2016)

Subregular hierarchy of maps



(Johnson, 1972; Kaplan and Kay, 1994; Mohri, 1997; Chandlee, 2014; Chandlee et al., 2017)

Computational complexity of phonological maps

REGULAR RELATIONS (Johnson, 1972; Kaplan and Kay, 1994)



SUBSEQUENTIAL FUNCTIONS (Mohri, 1997)



TIER-BASED STRICTLY LOCAL FUNCTIONS (Chandlee et al., 2017)

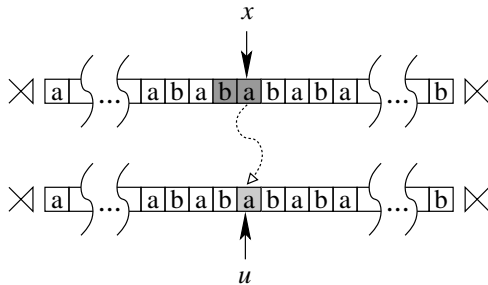


STRICTLY LOCAL FUNCTIONS (Chandlee, 2014)

Strictly Local functions

- ▶ Output string is computed *locally*, depending only on a bounded number of previous segments.
- ▶ Two varieties:
 - ▶ Input Strictly Local: output depends on previous input symbols
 - ▶ Output Strictly Local: output depends on previous output symbols

Input Strictly Local (ISL) function



Example: Input Strictly Local (ISL) function

- (1) Korean (Lee and Pater, 2008)
/pap**mul**/ \mapsto [pam**mul**] ‘rice water’

⊗ p a p m u l ⊗
λ

Example: Input Strictly Local (ISL) function

- (1) Korean (Lee and Pater, 2008)
/papmul/ \mapsto [pammul] 'rice water'

⊗ p a p m u l ⊗
λ pa

Example: Input Strictly Local (ISL) function

- (1) Korean (Lee and Pater, 2008)
/papmul/ \mapsto [pammul] ‘rice water’

⊗ p a p m u l ⊗
λ pa λ

Example: Input Strictly Local (ISL) function

- (1) Korean (Lee and Pater, 2008)
/pap**mul**/ \mapsto [pa**mmul**] ‘rice water’

×	p	a	p	m	u	l	×
	λ	pa	λ	mm			

Example: Input Strictly Local (ISL) function

- (1) Korean (Lee and Pater, 2008)
/pap**mul**/ \mapsto [p**ammul**] ‘rice water’

×	p	a	p	m	u	l	×
	λ	pa	λ	mm	u		

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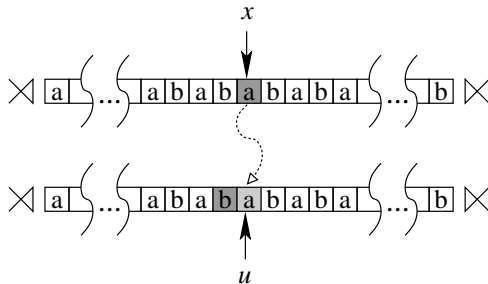
×	p	a	p	m	u	l	×
	λ	pa	λ	mm	u	l	

Example: Input Strictly Local (ISL) function

- (1) Korean (Lee and Pater, 2008)
/pap**mul**/ \mapsto [pam**mul**] ‘rice water’

Window size is 2: this map is 2-ISL.

Output Strictly Local function



Example: Output Strictly Local (OSL) function

- (2) Johore Malay (Onn, 1980)
/pəŋawasan/ \mapsto [pəŋãwãsan] ‘supervision’

× p e ŋ a w a s a n ×
p

Example: Output Strictly Local (OSL) function

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×	p	e	ŋ	a	w	a	s	a	n	×
	p	e	ŋ	ã	ã					

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	p	e	ŋ	ã	w̃	ã				

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×	p	e	ŋ	a	w	a	s	a	n	×
	p	e	ŋ	ã	wã	ã	s			

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	p	e	ŋ	ã	wã	ã	s	a		

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	p	e	ŋ	ã	wã	ã	s	a	n	

Example: Output Strictly Local (OSL) function

- (2) Johore Malay (Onn, 1980)
/pəŋawasan/ \mapsto [pəŋãwãsan] ‘supervision’

Window size is 2: this map is 2-OSL.

Long-distance (unbounded) assimilation

- (3) Kikongo (Meinof, 1932; Odden, 1994; Rose and Walker, 2004)
- a. /**tunikidi**/ \mapsto [tunikini] ‘we ground’
 - b. /kud**umukisila**/ \mapsto [kud**umukisina**] ‘to cause to jump
for’

Long-distance (unbounded) assimilation

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× t u n i k i d i ×
t u n i k i n

× k u d u m u k i s i l a ×
k u d u m u k i s i l

Example: Tier-based Strictly Local (TSL) function

(4) Kikongo (Meinof, 1932; Odden, 1994; Rose and Walker, 2004)

- a. /**tunikidi**/ \mapsto [tunikini] ‘we ground’
b. /kud**umukisila**/ \mapsto [kud**umukisina**] ‘to cause to jump
for’

► Designate a subset of the alphabet as the *tier*: $T = \{n, m, d, l\}$

× t u n i k i d i ×
t

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×	t	u	n	i	k	i	d	i	×
	t	u							

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	t	u	n						

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	t	u	n	i					

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	t	u	n	i	k				

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×	t	u	n	i	k	i	d	i	×
	t	u	n	i	k	i			

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
×	t	u	n	i	k	i	d	i	×
	t	u	n	i	k	i	n		

Long-distance assimilation with blocking

Slovenian (Jurgec, 2011; McMullin, 2016)

- a. **spi**f \mapsto **ʃpi**f ‘(you) sleep’
- b. **zaklɔniʃtʃe** \mapsto **ʒaklɔniʃtʃe** ‘bomb shelter’
- c. **nasiti**f \mapsto **nasiti**f ‘(you) feed’

- ▶ The blocking segments go on the tier.

× n a s i t i 

Long-distance assimilation with blocking

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- ▶ The blocking segments go on the tier.

× n a s i **t** i **ʃ** ×
 t i ʃ

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 i t i ʃ

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- c. $\text{nasit}\text{i}\text{f} \mapsto \text{nasit}\text{i}\text{ʃ}$ ‘(you) feed’

► The blocking segments go on the tier.

×	n	a	s	i	t	i	ʃ	×
			s	i	t	i	ʃ	

Example classifications

- ▶ ISL and OSL are argued to include all local phonological processes (assimilation, dissimilation, insertion, deletion, metathesis) (Chandlee, 2014; Chandlee et al., 2015)
- ▶ Many morphological ‘maps’ are also ISL (Chandlee, under review)
- ▶ TSL is conjectured to include long-distance processes

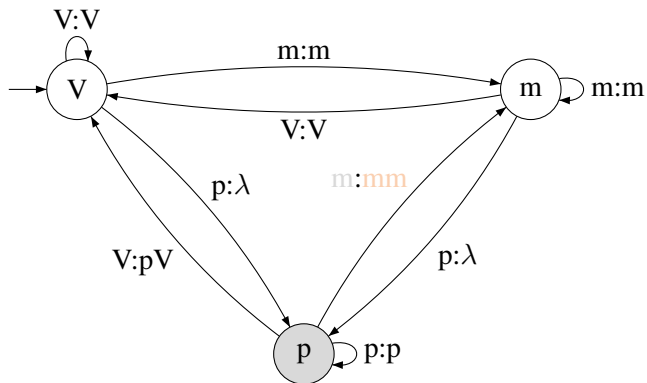
Characterizations

Class	Finite-state	Language-theoretic	Logical
ISL	✓	✓	✓
OSL	✓	✓	
TSL	✓	✓	

(Chandlee (2014); Chandlee et al. (2014, 2015, 2017), Chandlee and Lindell (to appear))

Input Strictly Local (ISL): FST characterization

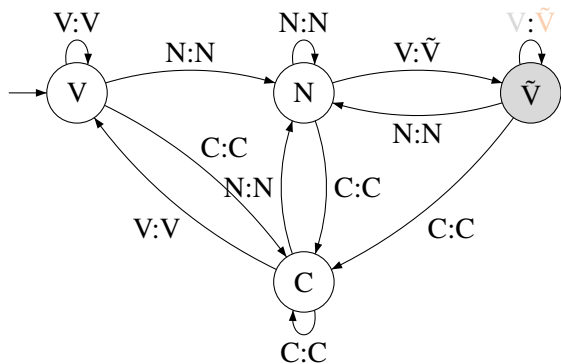
(5) /papmul/ \mapsto [pammul]



\times p a p m u l \times
 λ pa λ mm

Output Strictly Local (OSL): FST characterization

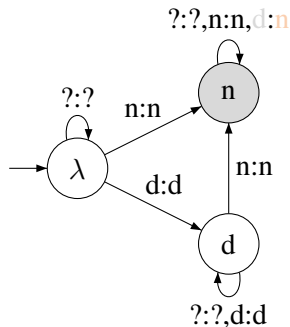
(6) /pəŋawasan/ \mapsto [pəŋãwãsan]



×	p	e	ŋ	a	w	a	s	a	n	×
	p	e	ŋ	ã	wã					

Tier-based Strictly Local (TSL): FST characterization

(7) /tunikidi/ \mapsto [tunikini]



⊗ t u **n** i k i **d** i ⊗
t u n i k i **n**

FST Characterizations

REGULAR RELATIONS (describable with FSTs)



SUBSEQUENTIAL FUNCTIONS (describable with deterministic FSTs)



TIER-BASED STRICTLY LOCAL FUNCTIONS (states are $T^{\leq k-1}$)



STRICTLY LOCAL FUNCTIONS (transitions follow recent input/output)

Map interactions

What about map interactions?

Case study: opaque phonological generalizations

- ▶ Opaque phonological generalizations result from the interaction of two processes: one is not ‘surface-true’.
- ▶ We’ve analysed the 7 distinct types of opacity from McCarthy (2007); Baković (2007); Kavitskaya and Staroverov (2010) and determined that all are ISL maps for some k .
- ▶ The needed information for determining the correct output at any point in the computation is found in a contiguous window of the input.

Case study: opaque phonological generalizations

- (8) Counterbleeding
- a. Lowering: [+long] \rightarrow [-high]
 - b. Shortening: V \rightarrow [-long] / $__ C \#$
- (9) Yokuts (McCarthy, 1999)
/ʔili:l/ \mapsto [ʔilel], ‘might fan’
- ▶ Lowering over-applies.

Case study: opaque phonological generalizations

(10) Counterbleeding

- a. Lowering: [+long] → [−high]
- b. Shortening: V → [−long] / C #

(11) Yokuts (McCarthy, 1999)

/ʔili:l/ ↦ [ʔilel], ‘might fan’

×	ʔ	i	l	i:	l	×
	ʔ					

Case study: opaque phonological generalizations

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	ʔ	i				

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	ʔ	i	l			

Case study: opaque phonological generalizations

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×	ʔ	i	l	i:	l	×
	ʔ	i	l	λ		

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	ʔ	i	l	λ	λ	

Case study: opaque phonological generalizations

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/ʔili:l/ ↦ [ʔilel], ‘might fan’

×	ʔ	i	l	i:	l	×
	ʔ	i	l	λ	λ	el

Case study: opaque phonological generalizations

- (12) Counterfeeding on environment
- a. Raising: $a \rightarrow i / _ CV$
 - b. Vocalization: $G \rightarrow V / C _ \#$
- (13) Bedouin Arabic (McCarthy, 1999)
- /badw/ \mapsto [badu], ‘Bedouin’
- ▶ Raising underapplies.

Case study: opaque phonological generalizations

- (14) Counterfeeding on environment
- a. Raising: $a \rightarrow i / _ CV$
 - b. Vocalization: $G \rightarrow V / C _ \#$
- (15) Bedouin Arabic (McCarthy, 1999)
/badw/ \mapsto [badu], ‘Bedouin’

×	b	a	d	w	×
	b				

Case study: opaque phonological generalizations

- (14) Counterfeeding on environment
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×	b	a	d	w	×
	b	λ			

Case study: opaque phonological generalizations

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	b	λ	λ		

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×	b	a	d	w	×
	b	λ	λ	ad	

Case study: opaque phonological generalizations

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×	b	a	d	w	×
	b	λ	λ	ad	u

Case study: opaque phonological generalizations

(16) Counterfeeding on focus

a. Deletion: $i \rightarrow \emptyset / _ CV$

b. Raising: $a \rightarrow i / _ CV$

(17) Bedouin Arabic (McCarthy, 1999)

/katab/ \mapsto [kitab], 'he wrote'

► Deletion underapplies.

Case study: opaque phonological generalizations

(18) Counterfeeding on focus

a. Deletion: $i \rightarrow \emptyset / _ CV$

b. Raising: $a \rightarrow i / _ CV$

(19) Bedouin Arabic (McCarthy, 1999)

/katab/ \mapsto [kitab], 'he wrote'

× k a t a b ×
k

Case study: opaque phonological generalizations

(18) Counterfeeding on focus

a. Deletion: $i \rightarrow \emptyset / _ CV$

b. Raising: $a \rightarrow i / _ CV$

(19) Bedouin Arabic (McCarthy, 1999)

/katab/ \mapsto [kitab], 'he wrote'

×	k	a	t	a	b	×
	k	λ				

Case study: opaque phonological generalizations

(18) Counterfeeding on focus

a. Deletion: $i \rightarrow \emptyset / _ CV$

b. Raising: $a \rightarrow i / _ CV$

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/katab/ \mapsto [kitab], 'he wrote'

×	k	a	t	a	b	×
	k	λ	λ			

Case study: opaque phonological generalizations

(18) Counterfeeding on focus

a. Deletion: $i \rightarrow \emptyset / _ CV$

b. Raising: $a \rightarrow i / _ CV$

(19) Bedouin Arabic (McCarthy, 1999)

/katab/ \mapsto [kitab], 'he wrote'

×	k	a	t	a	b	×
	k	λ	λ	it		

Case study: opaque phonological generalizations

(18) Counterfeeding on focus

a. Deletion: $i \rightarrow \emptyset / __ CV$

b. Raising: $a \rightarrow i / __ CV$

(19) Bedouin Arabic (McCarthy, 1999)

/katab/ \mapsto [kitab], 'he wrote'

×	k	a	t	a	b	×
	k	λ	λ	it	λ	

Case study: opaque phonological generalizations

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/katab/ \mapsto [kitab], 'he wrote'

×	k	a	t	a	b	×
	k	λ	λ	it	λ	ab

Case study: opaque phonological generalizations

(20) Self-destructive feeding (Baković, 2007)

a. Epenthesis: $\emptyset \rightarrow i / C(+)__C\#$

b. Deletion: $k \rightarrow \emptyset / V__+V$

(21) Turkish (Sprouse, 1997)

/bebek+n/ \mapsto [bebein], ‘your baby’

- ▶ Deletion destroys the environment for epenthesis.

Case study: opaque phonological generalizations

(22) Self-destructive feeding (Baković, 2007)

a. Epenthesis: $\emptyset \rightarrow i / C(+)_C\#$

b. Deletion: $k \rightarrow \emptyset / V_+V$

(23) Turkish (Sprouse, 1997)

/bebek+n/ \mapsto [bebein], ‘your baby’

× b e b e k + n ×
b

Case study: opaque phonological generalizations

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/bebek+n/ \mapsto [bebein], ‘your baby’

×	b	e	b	e	k	+	n	×
	b	e						

Case study: opaque phonological generalizations

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×	b	e	b	e	k	+	n	×
	b	e	b					

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	b	e	b	e				

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a. Epenthesis: $\emptyset \rightarrow i / C(+)__C\#$

b. Deletion: $k \rightarrow \emptyset / V__+V$

(23) Turkish (Sprouse, 1997)

/bebek+n/ \mapsto [bebein], ‘your baby’

×	b	e	b	e	k	+	n	×
	b	e	b	e	λ			

Case study: opaque phonological generalizations

(22) Self-destructive feeding (Baković, 2007)

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	b	e	b	e	λ	λ	λ	in

Case study: opaque phonological generalizations

- (24) Non-gratuitous feeding (Baković, 2007)
- a. Vowel epenthesis: $\emptyset \rightarrow V_i / \# _ \text{CCV}_i$
 - b. Glottal epenthesis: $\emptyset \rightarrow ? / \# _ \text{V}$
- (25) Classical Arabic (McCarthy, 2007)
- /ktub/ \mapsto [ʔuktub], ‘write.MASC.SG!’

×	k	t	u	b	×
	λ				

Case study: opaque phonological generalizations

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(25) Classical Arabic (McCarthy, 2007)

/ktub/ \mapsto [ʔuktub], ‘write.MASC.SG!’

×	k	t	u	b	×
	λ	λ	ʔuktu		

Case study: opaque phonological generalizations

(26) Cross-derivational feeding (Baković, 2007)

- a. Epenthesis: $\emptyset \rightarrow i / K_i _ K_i$
- b. Assimilation: $K \rightarrow [+voice] / _ D$

(27) Lithuania (Odden, 2005)

- a. /at-taiki:ti/ → [atitaiki:ti], ‘to make fit well’
- b. /ap-gauti/ ↦ [abgauti], ‘to deceive’
- c. /ap-berti/ ↦ [apiberti], ‘to strew all over’

×	a	p	b	e	r	t	i	×
	a	λ	pib					

Case study: opaque phonological generalizations

(28) Fed Counterfeeding (Kavitskaya and Staroverov, 2010)

- a. Glottalization: $\{t, d, s, n, \eta\} \rightarrow ? / _ \#$
- b. Deletion: $\Lambda \rightarrow \emptyset / _ (?) \#$

(29) Tundra Nenets

- a. $/tas\Lambda/ \mapsto [tas]$, ‘whole’
- b. $/t^j imj\Lambda s/ \mapsto [t^j imj?]$, ‘it rotted’

×	t	a	s	Λ	×	×	t ^j	i	m	j	Λ	s	×
	t	a	λ	λ	s		t ^j	i	m	j	λ	λ	?

Summary

Opacity Type	Language	<i>k</i>-value
cross-derivational feeding	Lithuanian	$k = 2$
counterbleeding	Yokuts	$k = 3$
fed counterfeeding	Tundra Nenets	$k = 3$
counterfeeding on environment	Bedouin Arabic	$k = 3$
counterfeeding on focus	Bedouin Arabic	$k = 3$
non-gratuitous feeding	Classical Arabic	$k = 4$
self-destructive feeding	Turkish	$k = 5$

Future work

- ▶ Complete the hierarchy of subregular maps
- ▶ Other types of map interaction
 - ▶ Blocking
 - ▶ Co-existing long-distance maps with and without distinct tiers

Conclusion

- ▶ There is an increasing amount of evidence that phonological patterns are subregular in nature, and this property is not dependent on analyses of individual generalizations.
- ▶ The class of ISL functions has been proven to be learnable from positive data (Chandlee et al., 2014; Jardine et al., 2014), and the analyses presented categorize opaque interactions as ISL.

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